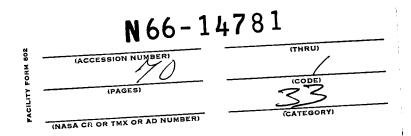
NASA TECHNICAL MEMORANDUM

NASA TM X-53346

October 18, 1965

NASA TM X-53346



A SET OF EXPERIMENTS IN THERMAL SIMILITUDE

by BILLY P. JONES AND JAMES K. HARRISON Research Projects Laboratory

NASA

George C. Marshall Space Flight Center, Huntsville, Alabama

GPC / mr	3
CFST# DARGE(S)	s
	2 0
Hard occy (H	c) <u>3.10 </u>
Was ≥ se (M	14
MOTO III	

NASA-GEORGE C. MARSHALL SPACE FLIGHT CENTER

TECHNICAL MEMORANDUM X-53346

October 18, 1965

A SET OF EXPERIMENTS IN THERMAL SIMILITUDE

by

Billy P. Jones

and

James K. Harrison

SPACE THERMODYNAMICS BRANCH
RESEARCH PROJECTS LABORATORY
RESEARCH AND DEVELOPMENT OPERATIONS

ACKNOWLEDGMENTS

The Arnold Engineering Development Center/ARO, Inc. fabricated the models and carried out the experiments in their facilities according to detailed specifications furnished by the Research Projects Laboratory, Marshall Space Flight Center.

Mr. Emerson Whatley, Scientific Programming, General Electric Company/Computation Laboratory, Marshall Space Flight Center, programmed the analysis of the experimental data on the IBM 7090 computer and the automatic plotting on the Stromberg-Carlson SC 4020 plotter.

TABLE OF CONTENTS

	Pa	ge
INTRODUCTION	. 2	2
DESCRIPTIVE EQUATIONS	. 3	3
SCALING RELATIONS AND MODEL DESIGN	. 3	3
EXPERIMENTAL APPARATUS AND PROCEDURES	. 9)
RESULTS AND DISCUSSION	. 13	3
CONCLUSIONS	. 15	5

NOMENCLATURE

- C; = heat capacity of jth region
- T; = temperature of jth region
- T_k = temperature of kth region
- $(\dot{T}_{i} = \text{derivative of } T_{i} \text{ with respect to time})$
- C_{ki} = over-all conduction coefficient between regions k and j
- R_{kj} = over-all radiant coefficient for net radiative transfer from region k to j
- q = internal power dissipation in the jth region
- SA; = effective area of surface j to sun
- A = total area of surface j radiating to space
- ϵ_{i} = infrared emissivity of surface j
- α_{j} = absorptivity of surface j with respect to solar insolation
- S = solar constant
- σ = Stefan-Boltzmann constant
- F_{kj} = classical geometry factor for net radiation exchange based on Lambert's cosine law for diffuse radiation
- d, b, r_1 , r_2 , r_3 , r_4 , L, W, h = particular linear dimensions (Fig. 2)
- k; = thermal conductivity of jth region
- (ρc_ρ) = density-specific heat product for jth region (volumetric heat capacity)
- H = solar radiation and internal generation (= $q + \alpha A S$)
- t = time

TECHNICAL MEMORANDUM X-53346

A SET OF EXPERIMENTS IN. THERMAL SIMILITUDE

SUMMARY

The analysis and results for two sets of experiments in thermal scale modeling are presented. The prototype and model consist of a plate, cylinder, and sphere exchanging thermal energy by radiation only. They were located relative to one another in an unsymmetrical arrangement.

The experimental results generally confirm the modeling rules, with some exceptions in the details, due largely to an a priori assumption made regarding the volume partitioning of the objects to be modeled.

INTRODUCTION

Previously derived scale modeling laws [1] were used as the basis for the design of experiments in thermal similitude. The purpose of the experiments was to test the theoretical laws for the transient case where several bodies with geometrical shapes common to space vehicles exchange energy solely by thermal radiation. The three bodies, a sphere, a cylinder, and a flat plate, were in a particular asymmetrical, geometrical arrangement (Figure 1).

Experiments were conducted on both a full-scale prototype and a model, since the primary objective was to test the scaling laws. The main overall dimensions of the prototype were scaled a priori by $\frac{1}{2}$ and minor dimensions were deliberately distorted to satisfy the scaling relations.

An important secondary objective of the experiments was to discover practical difficulties in modeling and to develop techniques to overcome them.

Analysis for the comparison of the prototype and model temperatures was made on an IBM 7090 computer, and the graphs were machine plotted using a Stromberg-Carlson SC 4020 plotter.

Some modeling work done by Adkins that is very similar to this has been reported in the literature [2].

This report includes two sets of experiments which were conducted several months apart.

DESCRIPTIVE EQUATIONS

Since there was no conductive or convective heat exchange between the objects, only radiative exchange will be considered. They are assumed to be exposed to external radiation equivalent to solar radiation and to have heat dissipated internally. Part of the objective was to use the crudest possible physical partition of the bodies in order to determine the limits on crudeness for modeling. Toward this end, each object is represented by a single temperature. The difference equations describing their transient behavior under these conditions are [3]

$$C_{j} \frac{\Delta T_{j}}{\Delta t} = \sum_{k=1, k \neq j}^{4} R_{kj} (T_{k}^{4} - T_{j}^{4}) + q_{j} + \alpha_{j}^{S} A_{j} S, \quad (j=1, 2, 3)$$
 (1)

and

$$\frac{\Delta T_4}{\Delta t} = 0$$
, $T_4 = constant$,

since T_4 represents the chamber wall, which is maintained with liquid nitrogen at a fixed temperature.

SCALING RELATIONS AND MODEL DESIGN

The general similarity criteria which includes this special case is given by Eq. (4) in Reference [1]. From this list, with the additional definition

$$H_{j} = q_{j} + \alpha_{j}^{S} A_{j}^{S} S, j = 1, 2, 3.$$
 (2)

the following independent set of scaling ratios is obtained:

$$\frac{T_j}{T_k}, \frac{\epsilon_j \sigma A_j T_j^3 t}{C_j}, \frac{R_{kj} T_j^3 t}{C_j}, \frac{H_j t}{C_j T_j}.$$
(3)

If electrical resistance heaters are used to obtain the simulated heating effects of solar insolation, and if the space chamber is regarded as incorporated in the third ratio with its appropriate exchange coefficient, then the modeling ratios for the problem are

$$\frac{T_{j}}{T_{k}}, \frac{R_{kj}T_{j}^{3}t}{C_{j}}, \frac{q_{j}t}{C_{j}T_{j}} (j, k = 1, ..., 4).$$
(4)

The detailed dimensional notation used is shown in Figure 2. All major external dimensions are scaled by $\frac{1}{2}$. It is assumed that the materials are not changed from prototype to model, that the radiation geometry factors remain unchanged, that the temperatures of the model at a particular time are equal to the corresponding prototype temperatures at the same time, and that the thickness of the cylinder end caps are not changed from prototype to model. These a priori requirements are

$$T_{j}^{*} = T_{j} t^{*} = t (\rho c_{\rho})_{j}^{*} = (\rho c_{\rho})_{j}$$

$$L^{*} = \frac{1}{2}L r_{2}^{*} = \frac{1}{2}r_{2} h^{*} = \frac{1}{2}h (j = 1, 2, 3)$$

$$F_{kj}^{*} = F_{kj} W^{*} = \frac{1}{2}W r_{4}^{*} = \frac{1}{2}r_{4}$$

$$b^{*} = b$$
(5)

These requirements, together with the scaling laws [4], impose geometric distortion in the minor dimensions. The results, summarized in Table I, were used as the basis for the detailed model design.

It is economical to fabricate whenever possible from standard gage material. However, review of the modeling rules in Table I reveals that the minor dimension distortions (thicknesses) constitute one of the main aspects. In addition, standard gage thicknesses have an average tolerance of ±0.005 inches, (1.27 x 10⁻⁴ meters) and there is often non-uniformity within a particular stock sheet. To minimize these difficulties, it was decided that the larger objects (prototype) would be fabricated from gage stock, but that the thicknesses of the stock sheet used would be measured to the smallest possible tolerance prior to use. Then, these measured thicknesses would be used in the modeling relations to predict the dimensions required for the models. The models, which are small, would then be fabricated by machining and milling to the tolerance of ±0.001 inch (2.54 x 10 meters). This appeared to be the most economical approach without compromising the modeling laws. The resulting dimensions are shown in Table II.

Electrical resistance heaters were used to represent internal dissipation and solar insolation on the plate. The heat capacity of the heater would upset the modeling criteria if it is relatively large compared to the heat capacity of the plate. Devices for attaching the heater to the plate also contribute substantially to the heat capacity of the system. However, the heater in all its aspects could also be modeled. It was decided that it would be best to represent the plate by two parallel sheets, each having equal thickness. The heater would then be mounted between the plates by carefully designed connectors, and the heater

TABLE I

Explicit Modeling Criteria

Quantity	Model/Prototype	Remarks
T _j	1	a priori determined
t	1	a priori determined
F _{kj}	1	a priori determined
(ρc _ρ) _j	1.	a priori, material property
L	$\frac{1}{2}$	a priori, major dimension
w	$\frac{1}{2}$	a priori, major dimension
r ₂	$\frac{1}{2}$	a priori, major dimension
r ₄	$\frac{1}{2}$	a priori, major dimension
h	1/2	a priori, major dimension
q _j	1/4	
d	1	distorted (derived)
b	1	distorted (a priori)
r ₁	$\frac{1}{4}$ k ₁	distorted (derived)
r_3	$\sqrt{\frac{2}{2}}k_3$	distorted (derived)

where

$$k_1 = 2\left[2 - \left(\frac{r_2}{r_1}\right)^3\right]^{\frac{1}{3}}, \text{ and}$$

$$k_3 = \left[1 - \frac{1}{2} \left(\frac{r_4}{r_3}\right)^2\right]^{\frac{1}{2}}.$$

6

TABLE II

Detailed Dimensions of Prototype and Model

Dimensions	Р	rototyp	oe .		Model		
	Stock		Meas	sured	Measured		
	Inches (Mete	ers)	Inches	(Meters)	Inches	(Meters)	
L			28.364	(.72042)	14.182	(. 3602)	
W			15.709	(.3989)	7.854	(. 1995)	
d	0.1285 (.003	3264)	0.257	(.006528)‡	0.1285	(.003264)	
b	0.064 (.001	.626)	0.065	(.001651)	0.065	(.001651)	
h			7.726	(.1962)	3.832	(.09733)	
r	5.866 (.149	0)	5.880 [†]	(.1493)	2.877	(.07307)	
r	6.000 (.152	24)			3.000	(.07620)	
r ₃	1.706 (.043	33)	1.707	(.04336)	0.701	(.001780)	
r ₄	1.964 (.049	88)			0.982	(.02494)	

 $r_2 - r_1$ was measured 0.120 inches (.003048 m), $r_4 - r_3$ was measured 0.257 inches (.006528 m).

[‡]Measured value was 2d

itself would have a very small characteristic time and low heat capacity. The sandwich arrangement was to be used for both the prototype and model. This arrangement would have allowed an approximate scaling of the heaters according to the following reasoning. By the modeling rules, the area of one side of the model plate would be $\frac{1}{4}$ that of the prototype. Assuming that the same heater material in the same wiring arrangement is used for both the prototype and model, the heat capacity of the heater will be directly proportional to the area of one side of the plate in both. So, the heater heat capacity for the model will be $\frac{1}{4}$ of that of the prototype. Since the internal generation is also scaled by $\frac{1}{4}$, the ratio q_1/C_1 will not be affected by the heater. In all of the ratios $R_{1,1}/C_1$, C_1 is scaled by $\frac{1}{4}$, since $d^* = d$; there is also a $\frac{1}{4}$ overall scaling of the numerator, so these ratios would not be affected either. It turned out that the sandwich construction was too difficult, especially with regard to the heater construction and mounting. Therefore, grooves were made in the plates. The wiring was routed through the grooves which were then filled with a special thermally conductive and electrically insulating cement. Roughly speaking, the same reasoning applies as for the intended sandwich construction, except that in making the grooves the plate material was removed before the cement material was added. In this respect, it was to a great extent fortuitous that the detailed modeling criteria presented in Table I was used.

Welding was used to fabricate the cylinder and to mate hemispheres. The amount of material in these welds contributes to the heat capacity. In order to minimize error from this source, all welds were ground to the contour of the external surfaces and care was taken to prevent excessive accumulation of weld material on the inside.

The thickness of thermal coatings could contribute significantly to the heat capacity, especially in the very small models. This problem was solved by smoking the surfaces of both prototype and model with carbon black produced by an acetylene torch. Resulting emittances were 0.98 to 0.99, according to measurements.

Another anticipated difficulty was the crudeness of the volume partition of the objects to be modeled. The finer the partition, the closer the basic equations [1] (and consequently, the modeling ratios) represent the objects thermal properties. On the other hand, as the partition becomes finer, the number of ratios that must be satisfied increases rapidly and the model design becomes more complicated. The crudest possible partition was used here, and it was anticipated that this would cause difficulty in analyzing the experimental data if there were large temperature differences around the object. Since the sphere for the first set of tests was made of stainless steel, it was the object most likely to exhibit this effect.

EXPERIMENTAL APPARATUS AND PROCEDURES

Both prototypes and models were suspended in the vacuum chamber by long, low-conductivity, small-diameter cables to prevent conductive exchange between the objects and the chamber walls. The rectangular chamber was 1.524 x 1.524 meters in cross-section and 3.658 meters in length. Pressure in the chamber during all experiments was 10^{-4} mm Hg or less. The walls were covered with cryopanels which provided a low temperature inclosure. In addition, both prototype and model occupied the same place in the chamber and were oriented in the same

way to minimize chamber influence on the test objects. The models as they appeared when installed in the chamber are shown in Figure 3.

Two sets of experiments were conducted. In the first set, stainless steel spheres and a plate with heaters installed were used. In the second set, changes were introduced in the sphere to obtain a more uniform temperature; the sphere in which heaters were installed was fabricated from aluminum alloy.

The three test objects had a total of 34 thermocouples for the first set of tests and 25 for the second set. Seven thermocouples were used to monitor the vacuum chamber cryopanel temperatures. The individual thermocouple identification numbers and locations are listed in Table III and Figure 4. On Table III, thermocouple number 1 for the first experiment and number 1 for the second experiment are at the same location on the sphere. This is true for thermocouple numbers 1 through 11, but not for any thereafter. For example, thermocouple number 13 for the first experiment and number 12 for the second are at the same location on the sphere. The locations can be seen by referring to Figure 4 in which the thermocouple numbers refer to the first experiment only. A minimum number of carefully located thermocouples was specified in order to minimize the heat conduction through the wires and still obtain adequate information on the temperature differences on opposite sides of the sphere and the cylinder.

Power loads during the power-on phase of the experiments are listed in Table IV.

TABLE III Individual Thermocouple Identification Numbers and Locations

	Thermocoup	ole Number
	First	Second
Object	Experiment	Experiment
	1	1
	2	2
	3	3
	4	4
	5	5
	6	6
	7	7
Sphere	8	8
•	9	9
	10	10
	11	11
	12	
	13	12
	14	13
	15	14
·	16	15
	17	16
	18	17
	19	
Cylinder	20	w w
	21	
	22	<u> </u>
·	23	18
	24	19
	25	20
	26	21
	27	22
	28	23
Flat Plate	29	24
	30	
	31	25
·	32	25
	33	
	34	

Note: Thermocouples 1 through 11 are at the same location in both experiments. Thereafter, the numbers vary. For example, thermocouple #13 for the first experiment and thermocouple #12 for the second experiment are in the same location on the sphere, etc.

11

TABLE IV
Power Loads
(watts)

Object	Prot	otype	Мо	del	
	Set 1	Set 2	Set 1	Set 2	
Plate	1053	1053	264	264	
Sphere	0	400	0	100	
Cylinder	0	0	0	0	_

An important aspect of modeling in the transient case is the initial conditions of the experiments. The temperature distribution for both model and prototype must be the same at the start of the test (or, in general, if temperatures are scaled, then an analogous statement holds for homologous temperatures at zero time). The difficulties arise when considering the duplication of cryopanel cool-down and heater turn-on. In order to eliminate possible differences in individual cryopanel cool-down curves due to different ambient starting temperatures, nitrogen flow rates, and manifolding between panels, the following experiment sequence was specified and used. A vacuum was established, then for both prototype and model, heaters and nitrogen for the panels were activated simultaneously and the systems were allowed to go to practical equilibrium. (If the heaters were not also activated, the objects under experiment would go slowly to panel temperature, taking 12

much more time and possibly causing difficulty with heaters, paints, and instrumentation at the low temperatures that would be obtained). A detailed analysis of various conditions is given in Ref. [3]. These equilibrium conditions were considered to be the initial conditions for the experiments. Then, the actual experiment sequence was cooling from these initial conditions (heaters suddenly "off") for two hours, then heating (heaters suddenly "on") for two hours. The periodic nature of these experiments has the inherent advantage of eliminating or minimizing the initial conditions which act as transients in the system, and which are eventually damped out by the thermal inertia of the system.

RESULTS AND DISCUSSION

Figures 5-16 show the experimental results for the first set of experiments. In all such graphs, temperature is plotted as a function of time and each prototype and corresponding model temperature is plotted on the same graph. The results for all cylinder and plate temperatures are excellent, and the model temperatures would be entirely adequate for predicting prototype temperatures. Two of the temperatures for the sphere (Figures 6 and 8) are acceptable, the differences between prototype and corresponding model temperatures being less than 8°K. However, two of the model temperatures for the sphere (Figures 5 and 7) are not good predictors of the corresponding prototype temperatures. The reason for this is clear. One of them, thermocouple number 3 (Figure 7), is the one nearest the heated plate, and the other, thermocouple number 1 (Figure 5), is the one farthest away from the heated plate. The low conductivity of the stainless steel sphere, together with the asymmetric heating by radiation from the plate, is not

consistent with the crude volume partition of the sphere. In other words, the a priori assumption that the model sphere can be designed using a single representative temperature is too crude. This is shown clearly in Figure 29, in which all sphere temperatures are plotted on one graph. It should be noted that all curves have the proper general shape.

The experimental results for the second set of experiments are shown in Figures 17-28. Here the spheres were constructed of aluminum and had some power dissipation in them (Table IV) in an attempt to obtain more uniform sphere temperatures. The expected improvement was obtained (compare Figures 29 and 30). The model temperatures for the sphere may be used to predict the corresponding prototype temperatures with good results, as can be seen from Figures 17 through 20. The cylinder curves (Figures 21-24) are not as good in this experiment as they were in the first. Again, as can be seen by reference to the geometric arrangement (Figures'l and 3), the combined heating of the sphere and the plate with asymmetric relative locations makes the assumption of a single representative temperature for the cylinder somewhat questionable (Figures 31-32) although not nearly as much so as for the sphere. In addition, and perhaps more importantly, the initial conditions for the prototype and model were not properly established; this is shown clearly by the graphs. Furthermore, the results for the plate (Figures 25-28) are not nearly as good in the second experiment as in the first. This is surprising since both sets of experiments used the same prototype and model plates. Furthermore, the reason for these apparently anomalous results for plate cannot be due to the fact that the sphere was heated in one experiment and not in the other since all temperatures over the plate show this same effect. The heating 14

portion of the curves could be explained by overheating of the models, but this would not explain the cooling portion of the curves. However, both heating and cooling curves can be explained by a lower emissivity for the model than the prototype. Coatings for these were smoked-on carbon black, which handling removes easily, and it is plausible that some of the carbon black was inadvertently removed from the model plate. The results for the second set of experiments are also shown in Tables V, VI, and VII. They are self-explanatory.

CONCLUSIONS

- 1. The modeling laws are generally confirmed by the experiment.
- 2. The volume partitioning used here was too crude; the sphere should have been divided into at least four regions.
- 3. Electrical resistance heaters are very useful to simulate internal energy dissipation but are not entirely satisfactory to simulate incident radiation because they necessarily become a part of the objects to be modeled, requiring that they also must be modeled.
- 4. Considerable care must be used in obtaining proper initial conditions if model experiments are to be used to predict prototype temperatures in transient cases that are not periodic.

<u>SUMMARY OF THERMOCOUPLE READINGS FOR SECOND SET OF EXPERIMENTS. TEMPERATURES IN DEGREES KELVIN</u>

(FOR EACH TIME PROTOTUPE READING IS LISTED FIRST, MODEL READING NEXT AND DIFFERENCE BETWEEN THEY LAST)

THERMECBUPLE NUMBER

TABLE V (CONT.)

	1		j			;			ľ	į	İ	
	 	_										
	25	459 458 -1	459 458 -1	459 458 -1	459 458 -1	154 154 0	374 392 18	352 352 23	301 325 24	276 306 30	262 290 28	249 278 29
	72	463 458 5	463 458 2-	463 458 5 -	463 458 -5	458 -3	377 393 16	352	302 326 24	306	263 291 28	251 278 27
1	2	438 458 21	438 888 00	4 58 20 20	4.48 8.02 0.02	437 457 20	367 393 26	352 352 27	298 326 28	274 306 32	262 291 29	249 278 29
AT PLATE	2	443 452 9	443 452 9	442 452 10	45 45 10	3 5∺	362 389 27	349	293 323 30	269 304 35	256 289 33	244 277 33
FE	12	458 453 -5	459 453 - 6	459 453 - 6	458 453 - 5	458 452 6-	376 388 12	349 17	303 323 20	278 334 26	264 289 25	251 277 26
	22	449 453	453	449 452 3	453	448 452 4	367 388 21	323 349 26	296 323 27	272 304 32	259 289 30	247 277 33
<u>#</u>	13	302 321 19	303	305 326 21	307 327 20	328 328 20	306 324 18	298. 315 17	289 304 15	278 295 17	271 286 15	263 277 14
CYL INDER	97	301 322 21	303 324 21	304 327 23	326 328 22	307 329 22	305 324 19	315	289 305 16	278 294 16	270 286 16	262 277 15
6	1.1	308 323 15	310 326 16	312 328 16	313 329 16	333	311 325 14	322 316 14	293	282 295 13	275 286 11	267 277 113
	16	309 320 11	311 323 12	313 325 12	314 326 12	316 327 11	311 323 12	302 314 12	293 304 11	282 294 12	275 285 10	267 277 113
	2	475 463 463	481 457 -24	4 4 8 3 1 2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	484 458 -26	484 458 -26	435	394 371 -23	364	334 321 -13	318 304 -14	302 291 -11
	1	461 36	467 498 31	6 6 4 6 6 6 6 6 6	994	469 498 29	426 431 5	383	353 351 -2	324 328 4	309 310	294 296 2
	13	\$60 553 93	\$65 554 89	467 555 88	467 555 88	\$56 89	424 456 32	382 404 22	352 370 18	324 344 20	309 325 16	294 310 16
	27	462 346 116	467 346 121	469 331 138	470 347 123	470 347 -123	422 340 -82	381	352 341 -11	324 341 17	308 319 11	293
	=	464	574 575	472 476 4	473 476 3	474 674 3.	427 420 -7	384 378 -6.	353 348 -5	325 326 1	309 308 -1	294 295 1
	2	458 463 5	463 466 3	4 9 6 4 6 6	465 105 1	465 1 1 1	422 418 -4	381	351	323 325 2	308 307 -1	293 294 1
	-	454	459 462 3	462 463 1	463 0	694	422 415 -7	381	351 343 -8	323 321 -2	308 304 14	293 291 -2
SPHERE	-	59 4	4403 -7	4.72 464 -8	449	679	428 415 -13	384 373 -11	354	326 322 -4	310 305 -5	294
ľ	•	7 9 4 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	467 471	469 471 2	469 471 2	469 471 2	413	381 376 -5	352 346 -6	323 324 1	308 307 -1	293 293 0
-	5	458 471 13	464 472 8	467 472 5	468 472 4	472	422 417 5-	375	351	323 323 3	308 -2	293 292 -1
	•	461 -7	466 457 -9	469 458 -11	470 458 -12	471 458 -13	427	372	363	325 321 -4	309 304 -5	294 295 -3
	-	694	474 472 -2	477 473 -4	478 473 -5	478 5 - 5	431 418 -13	388 376 -12	356 -13	328 323 -5	312 306 -6	297 292 -5
	2	469 453 -16	474 456 -18	477 456 -21	£ 55 55 50 50 50 50 50 50 50 50 50 50 50 5	457 -20	429 412 -17	386 371 -15	355 342 -13	326 321 -5	311 304 -7	296 291 -5
	ŀ	154	466 -12	4 4 6 8 8 4 4 8 8 8 4 4 8 8 8 4 4 8 8 8 4 4 8 8 8 4 8	455 135 135	468 455 -13		381 370 -11	352 342 -10	324	309 303 -6	293 290 -3
		80 80 01£	90	100 100 015	0110 0116	120 120 01 F	HEATER 130 42 130 41 DIF -1	140 140 01F	150 150 016	160 160 170	170 170 DIF	100 100 01 F
												17

IABLE V (CON1.)	8 10 11 12 13 14 15 16 17	281 281 281 281 282 281 288 259 263 278 281 282 343 278 268 269	0 1 59 14 2 -13 9	270 270 270 270 271 271 278 253 253 253 272 274 276 341 288 277 272 264 264 264 264 11 11 6 -6 11 11	261 261 261 261 261 268 246 247 262 264 266 341 277 266 262 256 257 1 3 5 80 16 5 -5 10 10	253 253 253 253 253 253 263 241 241 256 258 259 341 269 259 256 251 252 3 5 6 88 16 6 -4 10 11	245 245 246 246 246 252 235 236 249 251 252 341 262 253 249 246 246 4 6 7 95 16 7 -3 11 10	239 239 239 239 240 239 256 231 231 244 246 247 341 256 248 244 242 242 5 7 8 102 16 9 -2 11 11	257 257 259 265 269 257 293 228 228 286 320 328 332 439 332 285 239 243	3 69 67 179 75 -8 11 316 321 328 333 317 352 229 391 389 332 504 402 353 242 75 68 4 174 85 1 13	371 373 379 382 384 374 404 235 234 469 439 430 256 258 889 66 53 346 529 449 406 25 21 20	413 415 422 422 423 418 443 244 243 443 447 458 332 544 483 436 264 267 30 32 36 -90 121 65 -7 20 24	434 436 444 442 443 440 462 255 253 454 456 468 346 551 492 448 275 279
385HaV	1 2 3 4 5 6 7	281 283 283 282 281 281 282	3 -4 -2 0 -3	200 27 0 272 273 271 273 270 271. 27 200 272 272 273 272 273 274 273 27 01F 2 9 0 1 3 4 2	210 261 262 263 261 261 261 261 26 210 262 262 253 262 263 264 263 26 DIF 1 0 0 1 2 3 2	226 253 254 255 253 253 255 25 220 256 256 257 256 257 257 256 25 01F 3 2 2 3 4 4 2	236 245 247 247 246 245 245 246 24 236 249 249 250 249 250 251 250 24 DIF 4 2 3 3 5 6 4	246 239 241 241 239 239 239 271 22 240 244 244 245 246 245 2 01F 5 3 5 5 5 7 -26	HERTER BN 250 264 271 268 266 263 258 25 250 282 283 237 284 313 304 290 20	F 18 12 29 18 53 46 32 1 326 308 332 323 321 319 319 1 349 351 357 352 369 572 359 1 23 43 35 29 65 53 40	382 387 387 376 376 378 381 402 403 421 405 435 435 467 20 16 34 29 58 44 86	280 422 432 429 418 417 420 422 4. 280 452 434 452 436 456 450 442 4. 01F 10 2 23 18 39 30 20	290 441 458 453 440 438 441 444 4

TABLE V (CONT.)

							!	İ					
	52	453 454	1	454	454 456 2	454 456 2	454	454 457 3	454 457 3	374 391 17	318 351 33	298 324 26	277 304 27
				1			1				l l		
	3 2		0 -3	458	6 4 5 6 1 2	6 458 6 456 0 -2	6 457 7 457	6 457 7 457 1 0	7 458 7 458	7 376 2 392 5 16	5 320 1 351 6 31	6 300 4 324 8 24	6 278 4 304 8 26
ATE	23		. 20	436	4 4 8 6 2 0 2 0 2 0 2 0 2 0 2 0 0 2 0 0 0 0 0	200	436	434	437	367	315	296 2 324 2 324	276 3 304 2 28
FLAT PLATE	22		=	438	438 450 12	438 450 12	438 451 13	451 13	438 452 14	363	349	322	303
1	12	452	1	454	454 451 -3	454 451 -3	454 452 -2	455 452 -2	454 452 -2	376 388 12	321 348 72	301 322 21	279 303 24
	20	111	5	451	444	451 7	444 452 8	444 452 8	444 452 8	367 388 21	313 348 35	294 322 28	273 303 30
8	19	256	32	266	304	313 33	286 315 29	291 318 27	321 32	295 318 23	288 310 22	282 301 19	274 291 17
CYLINDER	81	255	33	798 788 788	273 305 32	279 311 32	286 316 30	291 319 28	294 322 28	294 318 24	287	282 301 19	273 291 18
9	=	264	56	273 299 26	282 307 25	288 313 25	294 317 23	299 321 22	302 323 21	102 918 94	292 311 19	286 301 15	278 292 14
	16	266	2	274 296 22	283 203 20	289 309 20	295 314 19	299 ´ 317 18	303	317	292 309 17	286 303 14	276 291 13
	15	174		£ 52.7	475 458 -18	477 458 -19	477 459 -18	411 459 -18	478 453 -19	411	383	361 341 -23	334 319 -15
	1.4	154		5 8 5 4 5 5 4 5 4 5 4 5 4 5 4 5 4 5 4 5	458 498 40	864	8 6 C	85 G	39	429	15	348	324 329 5
	13	653	1	457 556 99	459 556 97	55. 55. 56.	459 98	557 79	\$55 98	386	368 35	347	323
	12	452		456 346 110	458 112	459 332 -127	459 346 -113	332 332 -127	113	417 -77	367 340 -27	34.7	323 341 18
	11	454 4		459 476 17 = 1	461 477 16 -1	462 4 477 3 15 -1	462 477 15 -1	478 16 -1	4 18 1 15 1 15 1 15 1 15 1 15 1 15 1 15	422 420 3	370 378	348	324 3
	10	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		159	153 4	454 465 11	454 4	454 466 12	11	117	367	346	322 324 3
	80	4 544	1	450 4 463 4	452 4 464 4 12	453 465 112	453 466 13	454 466 466 4	454 4 466 4 12	4 10 4	367 3	346 3	323 321 321
SPHERE	7		l	- 1			1		İ	1			
SP	۰	454		6 459 0 463	17 462 4 464 4 2	462 464 464 464	2 465 4 209	9 463 3 466	50 463 3 466 3 3	8 422 9 415 1 -7	7 371 6 373 9 2	7 349 5 343 2 -6	3 324 3 321 0 -3
		154 6	1	3 456 1 470 14	471 41	5 458 2 472 5 14	458 472 5 14	459	2 4 7 2 4 2 5 2 4 2 5 4 2	419	7 367	347	2 323 1 323 0 0
		97	1	453 471 18	456 472 16	456 472 16	457	452	152	714	357	34.7	322
	•	452		457 457 0	459 458 -1	460 459 11	459	461	461 460 1-	421 413 -8	370 371	342	324 320 -4
	9	194	1	465 473 B	467 474 7	468 474	468	468	468 476 8	427 418 -9	374	352	327 322 -5
	2	124	-19	476 455 -21	478 456 -22	478 457 -21	479 457 -22	479 458 -21	479 458 -21	f 431 411 -20	¥25.	352	327 319 -8
	-	\ £:	0	455 453	154 484 4.	458 455 -3	456 456	456	\$ \$ \$ \$ £ .	ER 86	368 369	341	324 319 -5
	i	300	910	310 310	320 320 01f	330 330 01F	340 340 01F	350 350 01F	360 360 01F	370 4 370 4 01F	380 380 01 F	390 390 DIF	34 30 7
				}						1			19

TABLE V (CONT.)

- : 1							1	i	
	25	263 289 26	252 277 25	242 267 25	234 258 24	231 251 20	221 246 25	216 243 24	212 236 236
	24	264 289 25	253 277 24	243 267 24	235 258 23	232 252 20	222 246 24	217 241 24	212 236 24
FLAT PLATE	23	263 289 26	252 277 25	242 267 25	234 259 25	231 252 21	221 246 25	216 241 25	211 236 25
	22	258 288 30	247 276 29	238 266 28	231 258 27	228 251 23	218 245 27	214 240 26	209 236 27
	21	266 288 22	254 276 22	244 266 22	236 258 22	232 251 19	222 245 23	217 240 23	213 236 23
	20	260 288 28	249 276 .27	240 266 26	232 258 26	229 251 22	219 245 26	215 240 25	212 236 26.
ER	19	268 282 14	261 274 13	255 267 12	249 261 12	247 255 8	239 250 11	234 246 12	229 242 13
CYLINDER	18	267 283 16	260 274 14	254 268 14	248 261 13	246 256 10	238 250 12	233 246 13	229 242 13
٥	11	271 283 12	265 274 9	258 268 10	253 261 8	253 256 6	242 251 9	238 246 8	233 242 9
	16	271 282 11	264 ° 274 13	258 267 9	253 261 8	253 255 5	242 250 8	237 245 8	233 242 9
	15	317	303 289 -14	293 278 -12	283 269 -11	275 262 -14	263 255 -8	257 243 -8	253 244 5
	*	308	294 296 2	283 284 1	273 275 2	268 267 -1	256. 259 3	253 253_ 3	243
	13	308 324 16	295 308 13	283 296 13	273 285 12	269 276 7	257 268 11	251 262 11	244 256 12
	12	308	294 340 46	283 340 57	273 339 66	269 339 70	256 339 83	250 339 89	244 340 96
	=	308 308	294 293 -1	283 282 -1	273 273 0	269 265 -4	256 258 2	250 252 2	243 248 5
	10	307 327 0	294 292 -2	282 281 -1	273 272 -1	268 264 -4	256 257 1	250 251 1	243 247 4
щ	8	357 364 -3	294 290 -4	282 279 -3	273 269 -4	268 262 -6	256 256 0	249 250 1	243 245 2
SPHERE	-	309	296 290 290	283 279 -4	274 270 24	269 262 -7	251 256 -1	251 250 250 -1	244 246 2
	۰	308	294 292 2	283 281 -2	273 271 2-2	268 263 -5	256 257 1	250 251 1	244 246 246 2
	~	307	294 291 -3	282 279 279	273 273 -3	268 262 -6	256 256 3	249 250 1	243 246 3
	4	309 3 13 -6	295 289 -6	283 278 -5	273 269 -4	268 262 -6	251 255 -2	250 249 -1	244 245 1
	6	311 325 -6	297 291 291	285 280 -5	275 271 271 -4	269 253 -6	258 256 -2	251 251 5	245 246 1
	7	311 322 -9	297 289 ±8	285 278 -7	275 269 269	271 262 -9	258 255 -3	252 249 249 -3	245 245
	1-	308	294 289 -5	283 278 -5	269	271 261 -10	25.7 25.7 0	250 249 -1	244
		416 416 016	420 420 01F	430 430 01F	110 314	450 450 01F	466 466 01 F	470 470 01F	480 480 01F
20)	i ! !			1			į	

TABLE VI

Fraction of Time in Percent where the Difference Between the Prototype

Fraction of Time in Percent where the Difference Between the Prototype and Model Temperatures of the Individual Thermocouple Measurements are Equal to or Less than 5, 10, 15, 20, and 25 Degrees Kelvin. †

Thermocoup Number	le 5	10	15	20	25
1	59.2	75.5	89.8	95.9	98.0
2	26.5	46.9	63.3	79.6	95.9
3	51.0	79.6	89.8	89.8	93.9
4	55.1	73.5	89.8	93.9	93.9
5	44.9	57.1	69.4	79.6	89.8
6	51.0	65.3	85.7	89.8	91.8
7	51.0	75.5	83.7	85.7	87.8
8	55.1	71.4	85.7	89.8	89.8
10	53.1	67.3	87.8	89.8	91.8
11	42.9	61.2	81.6	89.8	91.8
12	2.0	6.1	10.2	14.3	14.3
13	0.0	2.0	18.4	40.8	44.9
14	38.8	51.0	55.1	57.1	59.2
15	10.2	28.6	59.2	79.6	95.9
16	6.1	36.7	75.5	93.9	100.0
17	4. l	30.6	67.3	81.6	93.9
18	4.1	8.2	32.7	63.3	79.6
19	4.1	10.2	49.0	71.4	81.6
20	32.7	46.9	46.9	46.9	59.2
21	42.9	49.0	53.1	59.2	83.7
22	4.1	24,5	46.9	46.9	49.0
23	2.0	2.0	2.0	26.5	65.3
24	44.9	46.9	46.9	57.1	77.6
25	46.9	46.9	46.9	53.1	73.5

†Determined from discrete points in time corresponding to data readout times.

TABLE VII

NUMBER OF DIFFERENCES LESS THAN OR EQUAL TO
5, 10, 15, 20, and 25 DEGREES KELVIN AT VARIOUS TIMES

			OOG 1110	ILO			
	TIME-MIN	5	10	15	20	25	
ĺ	Ö	6	6	23	23	23	
}	10 20	1	4 11	9 16	11 20	17 22	
	30	10	15	17	18	22	
	40	12	15	19	19	21	
	50 60	8 8	14 13	18 19	18 20	20 22	
	70	8	12	16	20	21	
	82	8	14	17	19	21	
	90	8	13	15 15	18	21	
	100	9	12	15	17	21	
	110	10	12	15	19	20	
	120 130	9	11 6	15 13	19 18	20 20	
	140	3	6	13	16	25	
	150	3	9	15	18	21	
	160	11	11	14	18	18	
	170	8	12	16	18	19	
	180	11	13	16	17	17	
	190 200	11	14 12	17	17 17	17	
	210	11	14	15 15	17	17	
	220	io	13	16	17	17	
	230	9	14	16	18	18	
	240	6	11	14	16	16	
	250	0	1 7	4	9	13	
	260 270	6	(9 6	119	13 12	
	280	5 5	8	8	11	14	
	290	5	7	11	15	17	
	300	6	8	10	16	18	i
	310	6	8	12	16	18	i
	320	6	8	12		19	
	330 340	6 5	8	13 13	17	19	
	350	6	7 8	13	15 16	18 19	
	360	6	8	14	17	19	
	370	5	10	īi	16	21	
	380	6	10	12	16	16	L
	390	6	11	14	17	20	l
	400	10	11	14	18	19	ĺ
	410	7	11	15	17	19	
	420 430	7 10	13 13	17 17	17	21	
	440	10_	13		17 17	21 21	İ
	450	5	16	17	20	23	Γ.
J	460	ıí	14	17	17	21	1
	470	11	14	17	17	22	1
	480	10	14	17	17	21	
							ı

REFERENCES

- 1. Jones, Billy P., "Thermal Similitude Studies," <u>Journal of Space-craft and Rockets</u>, Vol. 1, No. 4, July August 1964.
- 2. Adkins, D. L., "Scaling of Transient Temperature Distributions of Simple Bodies in a Space Chamber," AIAA Thermophysics Specialist Conference, Monterey, Calif., Sept. 13-15, 1965, AIAA Paper No. 65-660.
- 3. Jones, Billy P., "A Study of Several Numerical Methods for Solving a Particular System of Ordinary Differential Equations," NASA TMX-53121, August 5, 1964.

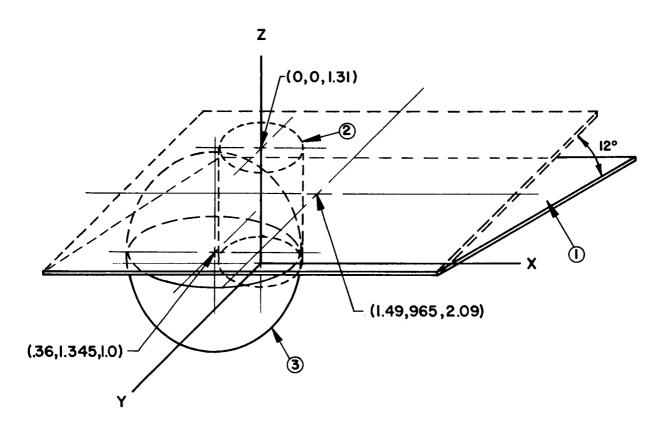


Figure 1 - Geometric Arrangement. Numbers shown are based on outside dimensions of sphere's radius. Coordinate system shown is centered at base of cylinder.

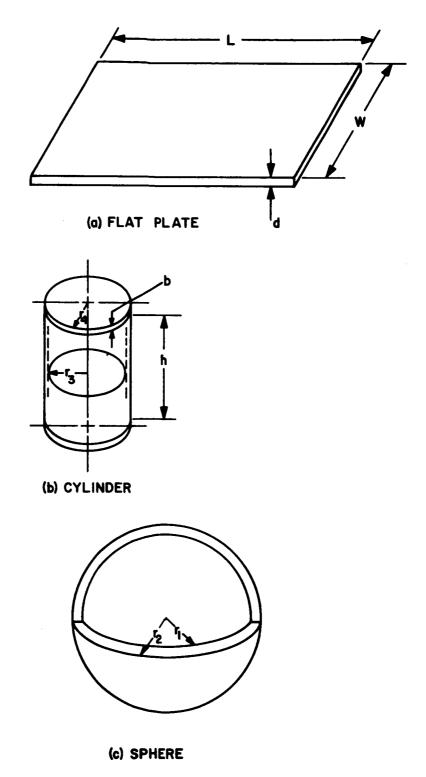


Figure 2 - Dimensional Notation-Numerical Values Given in Table II



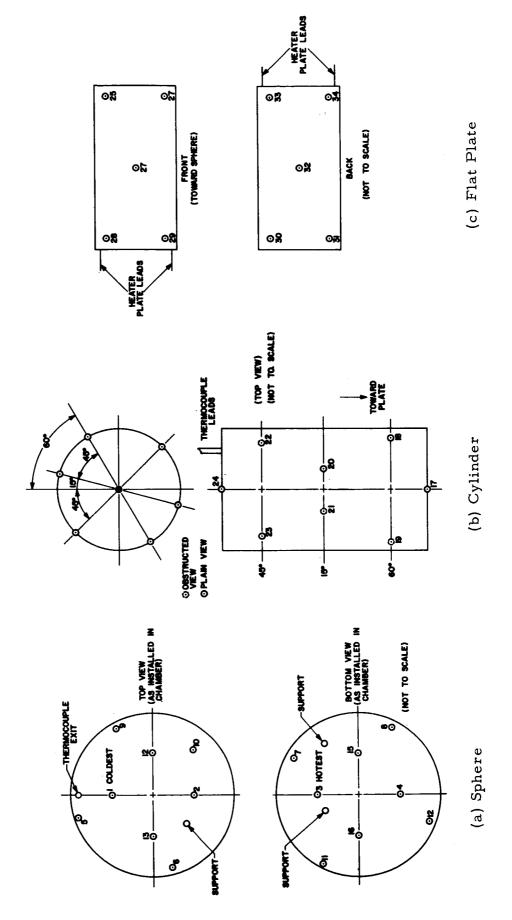
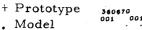


Figure 4 - Individual Thermocouple Identification Numbers and Locations (First Experiment only).



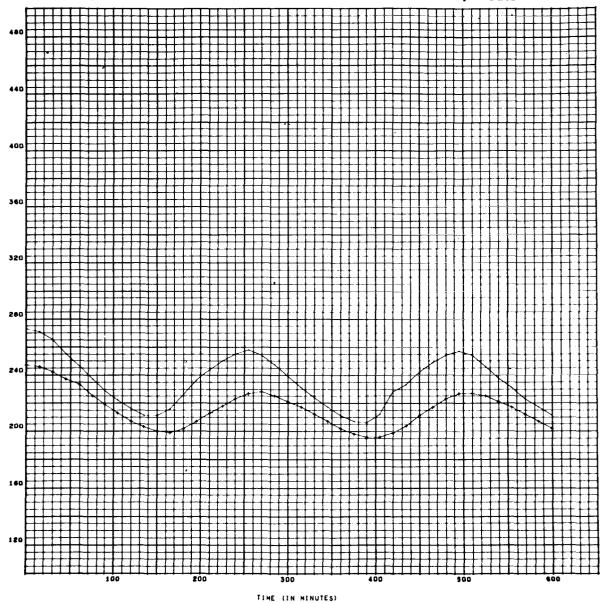


Figure 5 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 1 (First Experiment)

TEMPERATURE IN DEGREES KELVIN

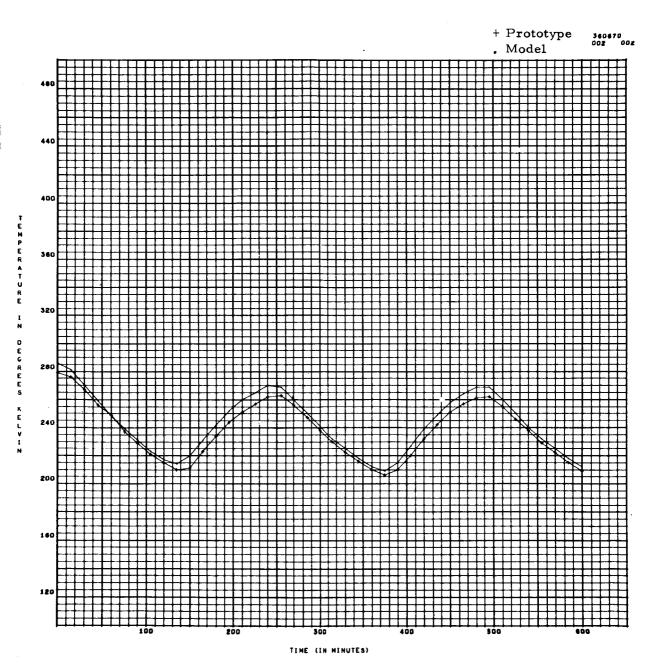
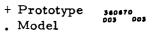


Figure 6 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 2 (First Experiment)



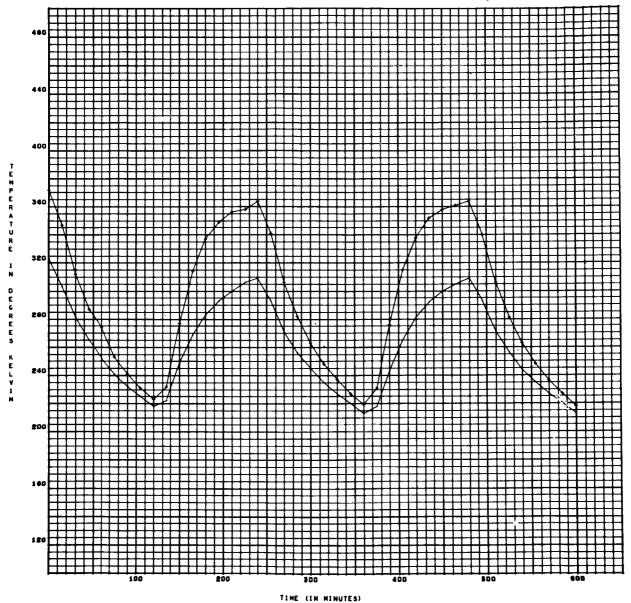
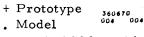


Figure 7 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 3 (First Experiment)



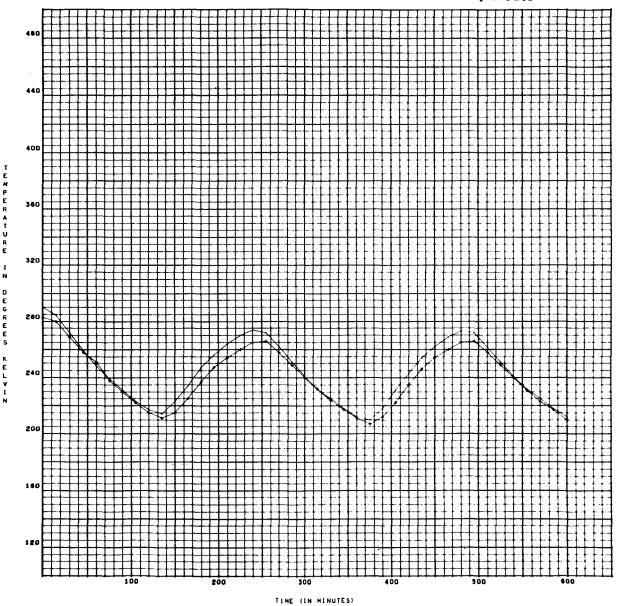
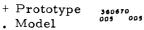


Figure 8 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 4 (First Experiment)



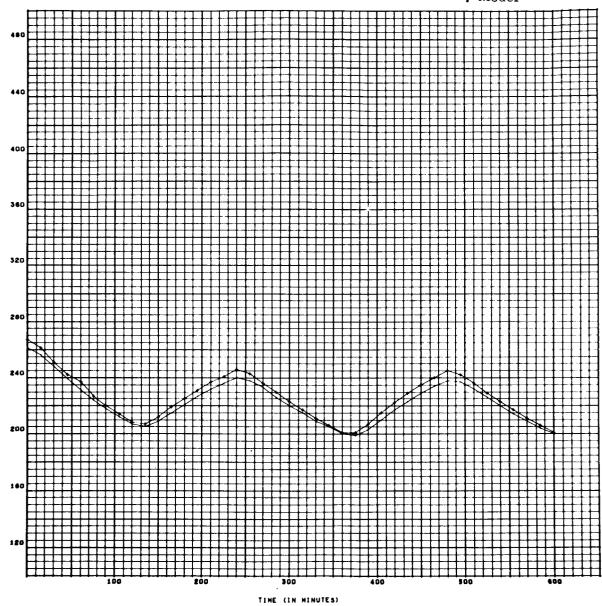


Figure 9 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 17 (First Experiment)

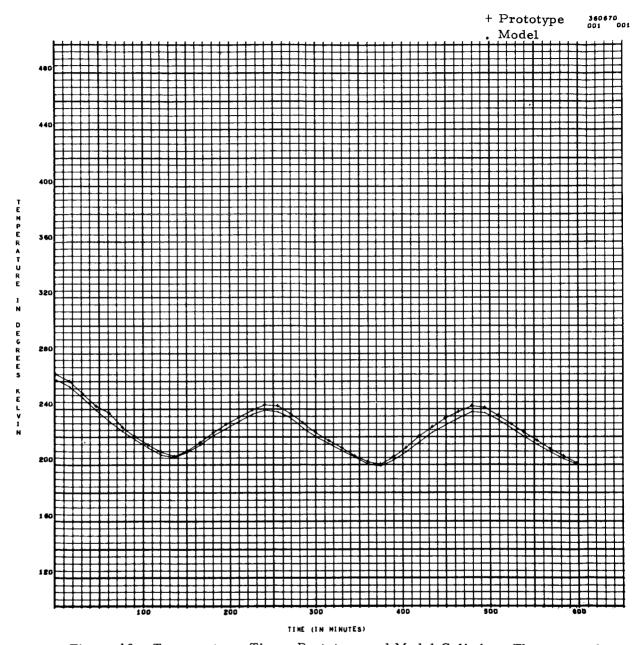
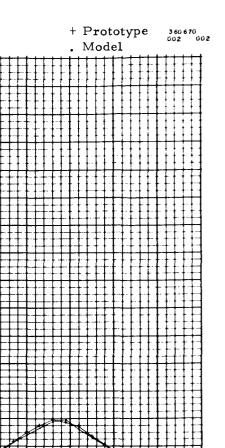
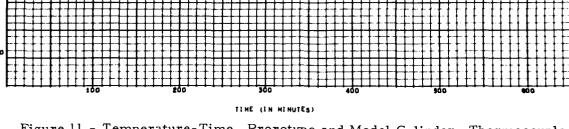


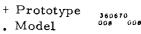
Figure 10 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 19 (First Experiment)





TE M P E R A T U R E

Figure 11 - Temperature-Time, Prorotype and Model Cylinder, Thermocouple
No. 22 (First Experiment)
34



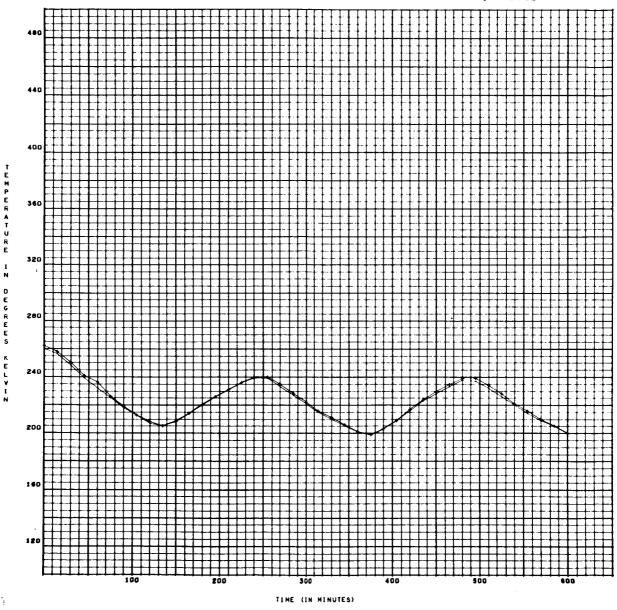


Figure 12 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 24 (First Experiment)
35

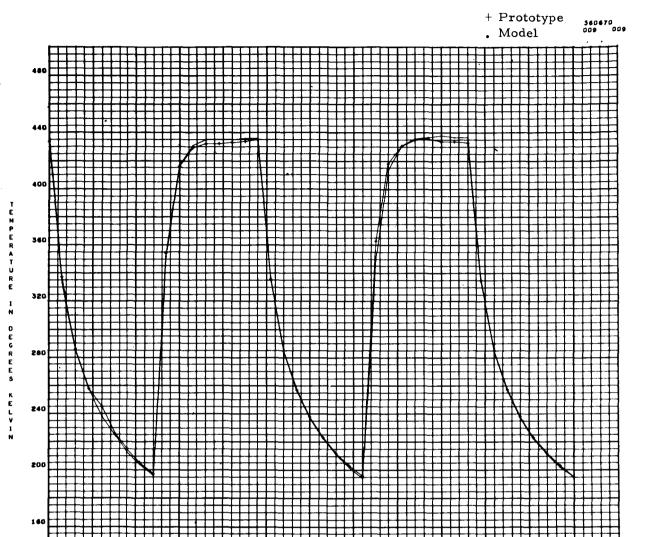
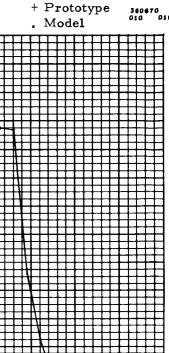


Figure 13 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 25 (First Experiment)

TIME (IN MINUTES)



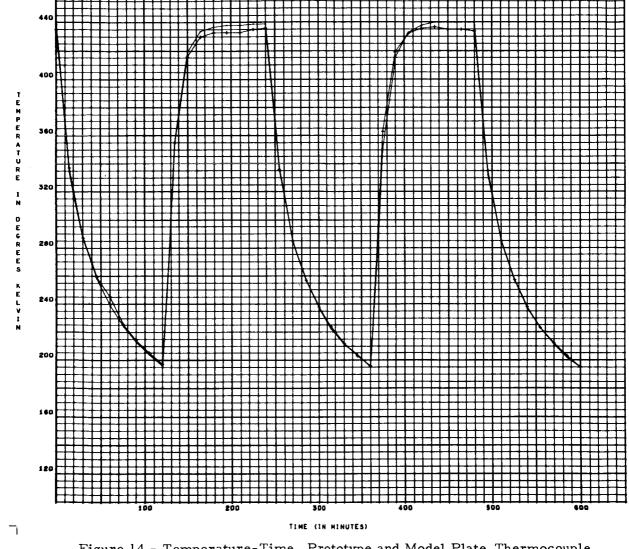
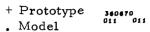


Figure 14 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 27 (First Experiment)



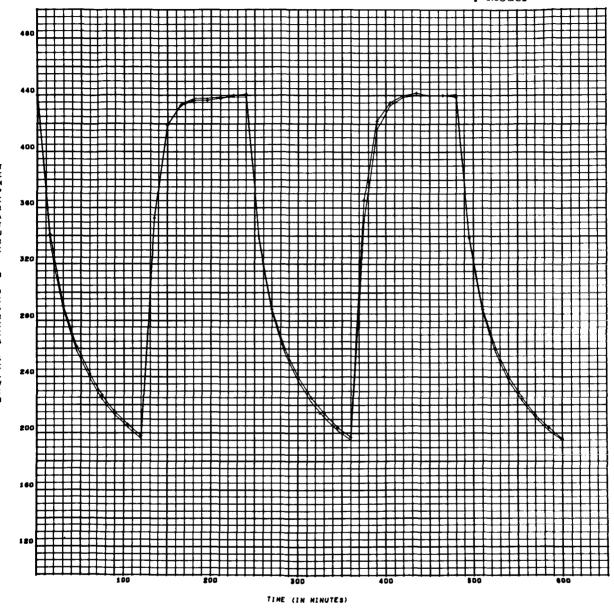


Figure 15 - Temperature-Time, Prototype and Model Plate, Thermocouple
No. 29 (First Experiment)

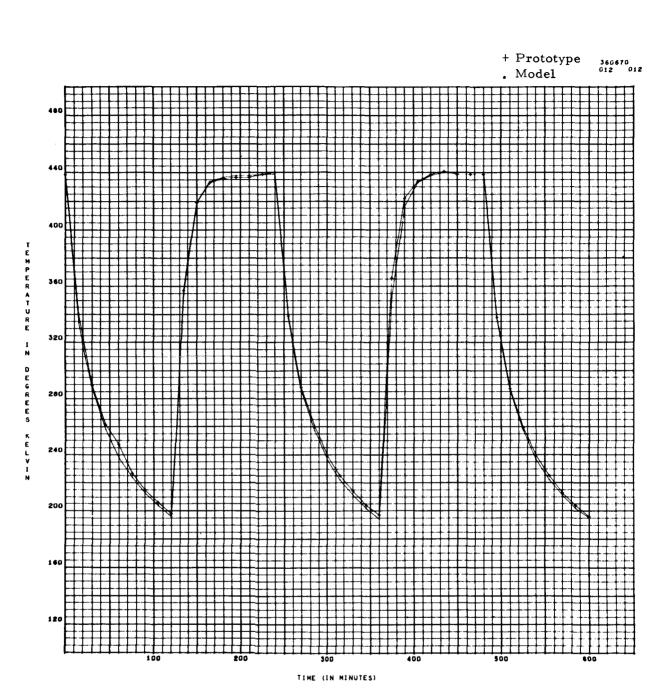
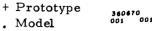


Figure 16 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 32 (First Experiment)



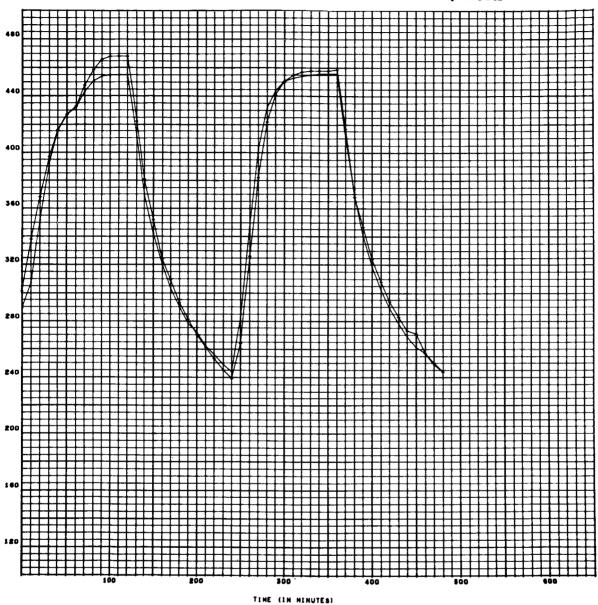
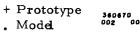


Figure 17 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 1 (Second Experiment)



. 41

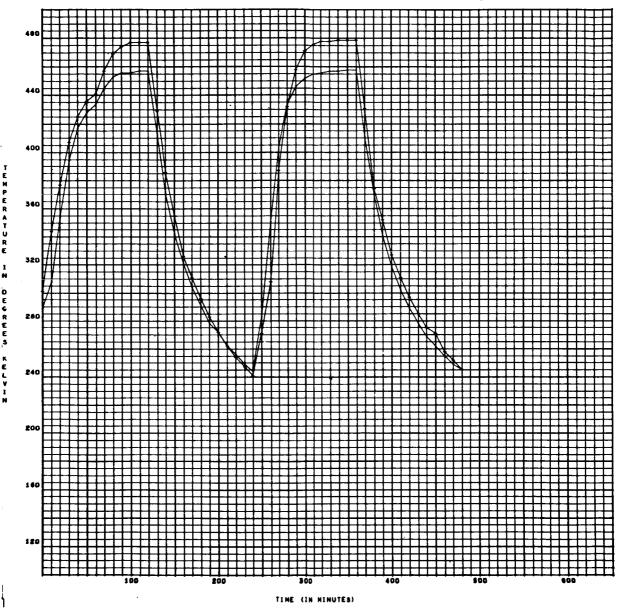
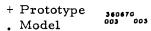


Figure 18 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 2 (Second Experiment)



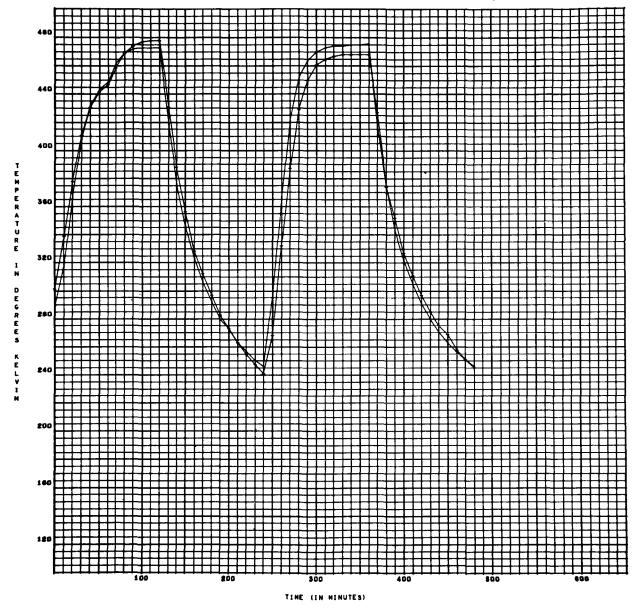
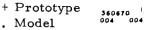


Figure 19 - Temperature-Time, Prototype and Sphere, Thermocouple No. 3 (Second Experiment)



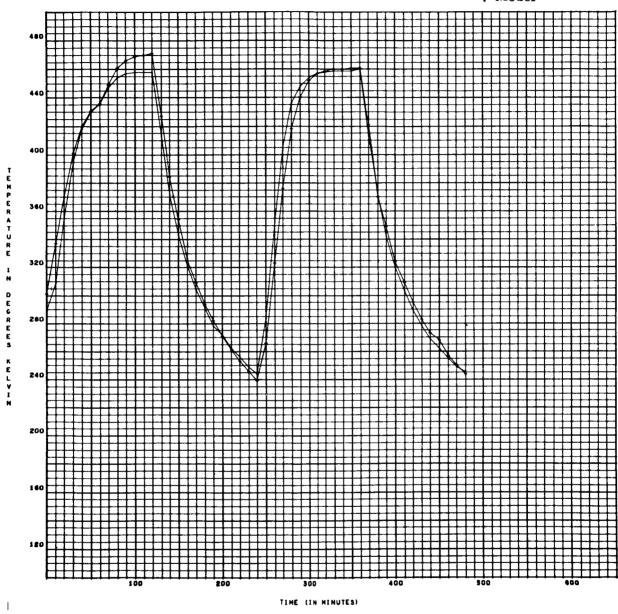
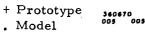
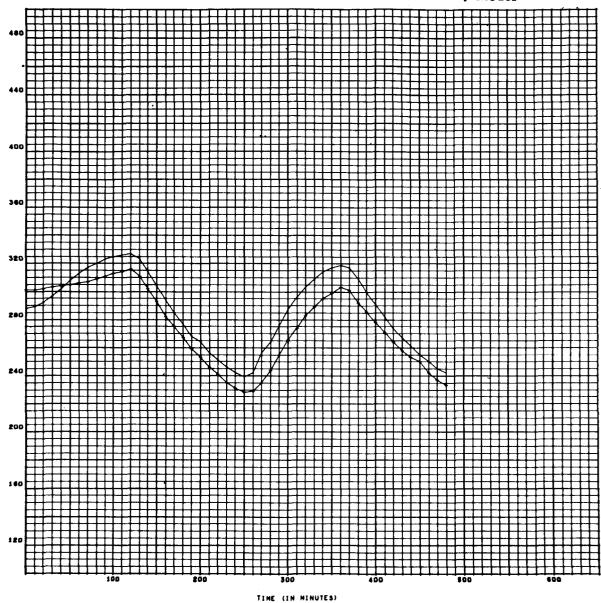


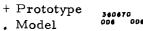
Figure 20 - Temperature-Time, Prototype and Model Sphere, Thermocouple No. 4 (Second Experiment)





TEMPERATURE IN DEGREES KELVIN

Figure 21 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 16 (Second Experiment)



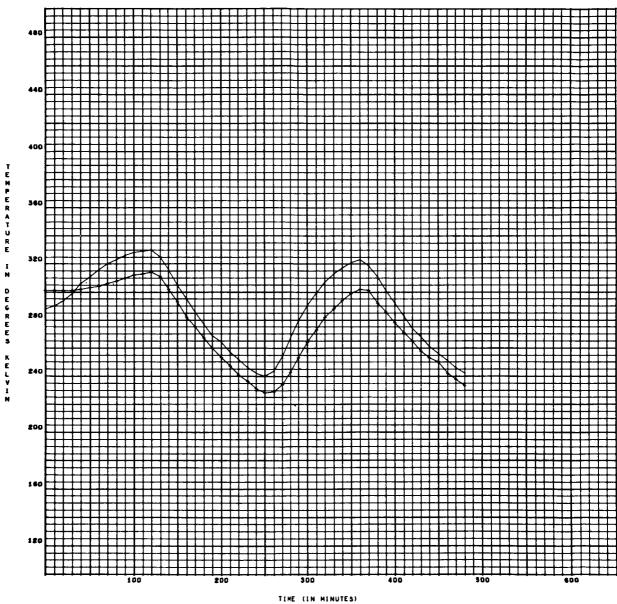
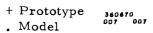


Figure 22 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 17 (Second Experiment)
45



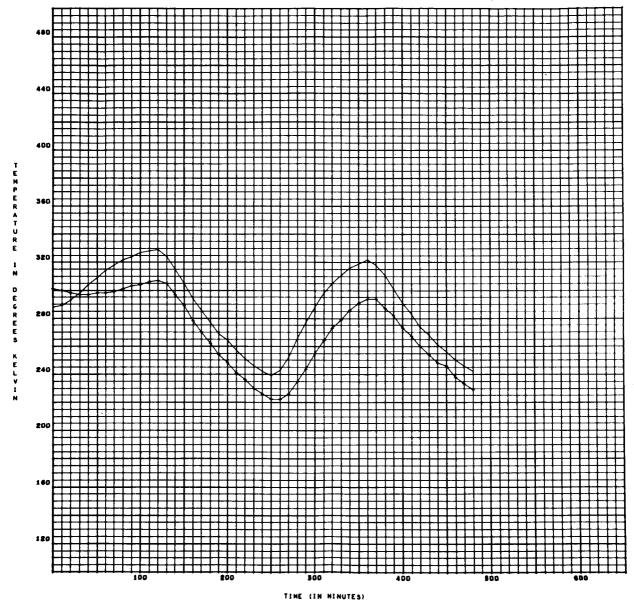
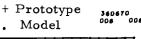


Figure 23 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 18 (Second Experiment)



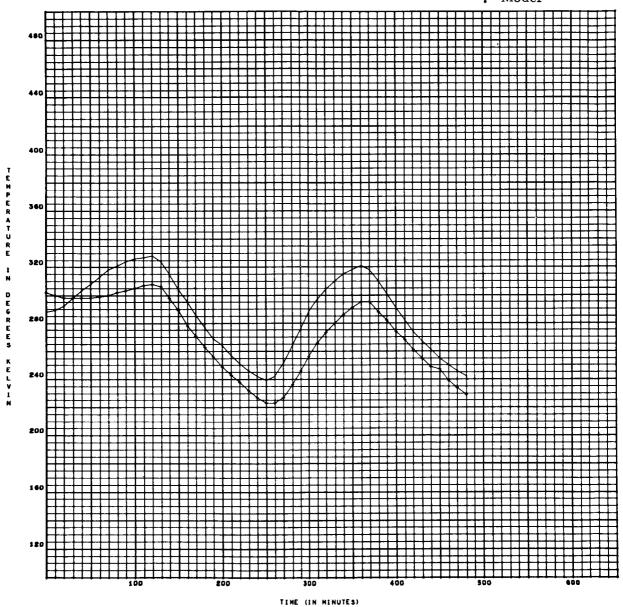
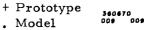


Figure 24 - Temperature-Time, Prototype and Model Cylinder, Thermocouple
No. 19 (Second Experiment)

47



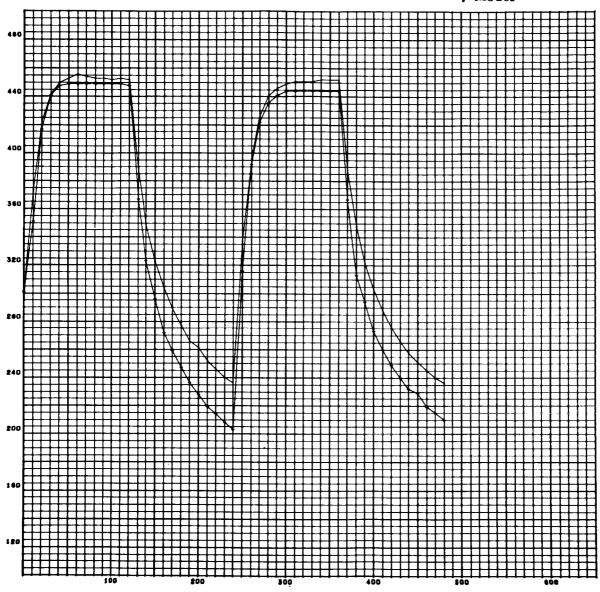
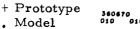


Figure 25 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 20 (Second Experiment)

TIME (IN MINUTES)



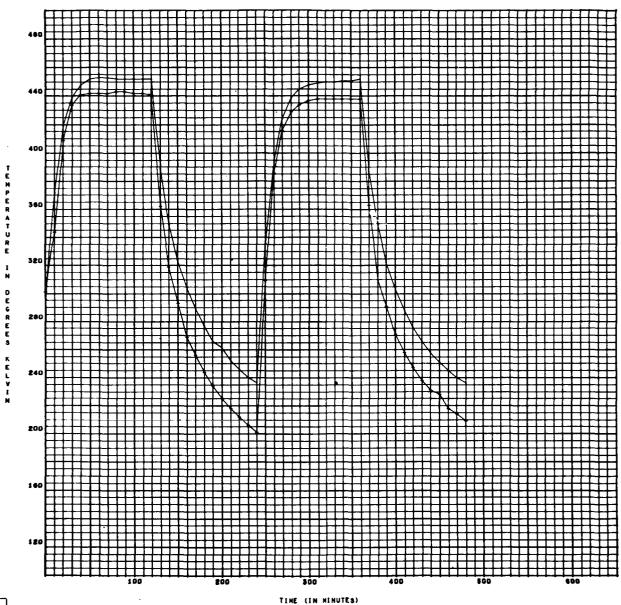
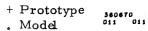


Figure 26 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 22 (Second Experiment)



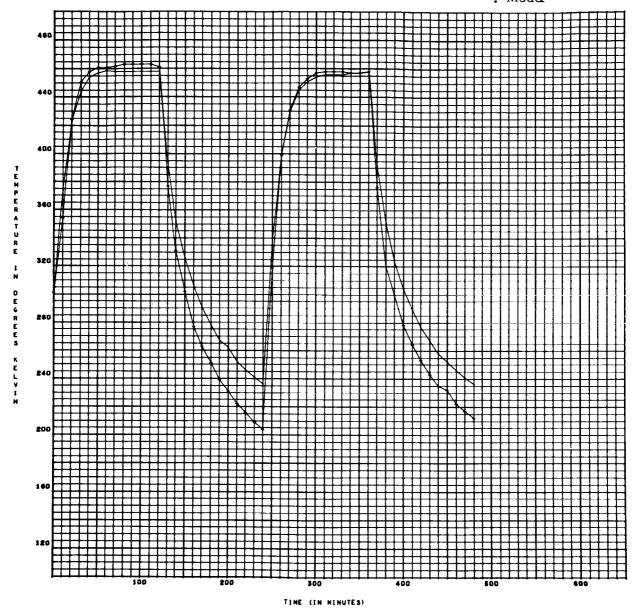
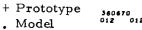


Figure 27 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 24 (Second Experiment)



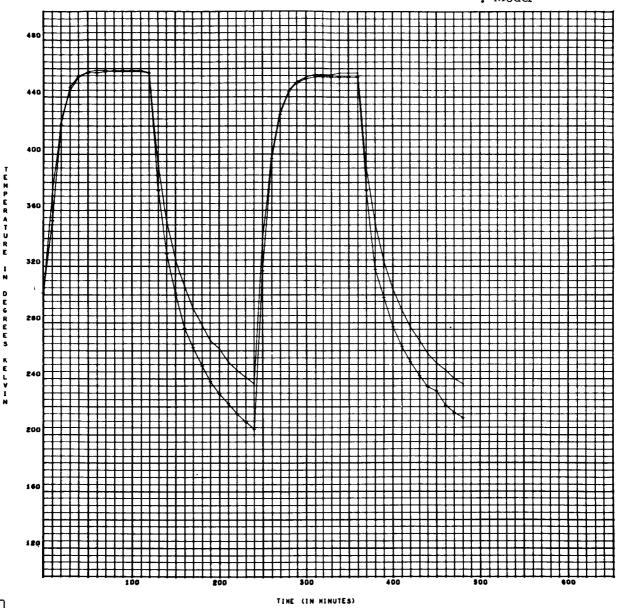


Figure 28 - Temperature-Time, Prototype and Model Plate, Thermocouple No. 25 (Second Experiment)

Figure 29 - Temperatures for Prototype Sphere for First Experiment 52



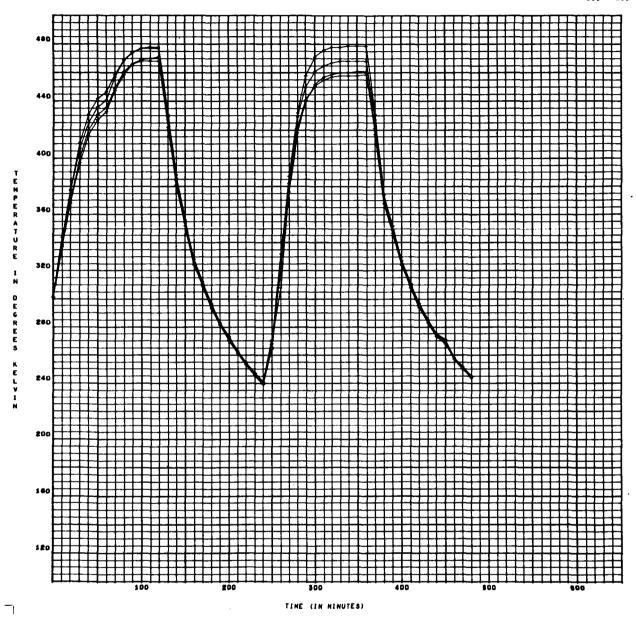


Figure 30 - Temperatures for Prototype Sphere for Second Experiment

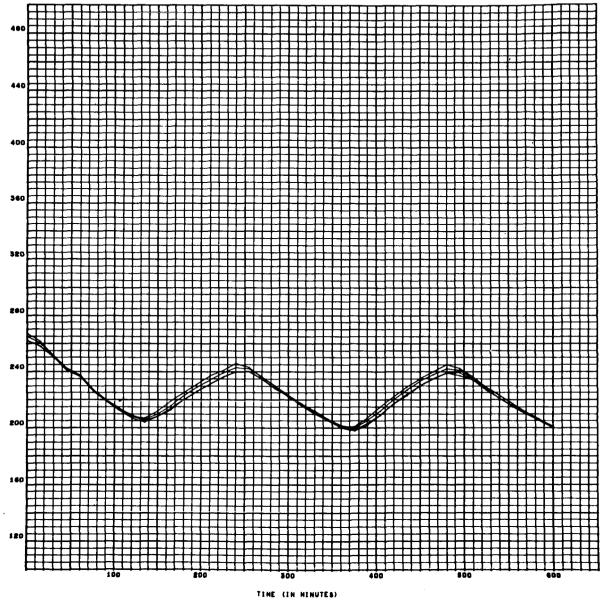


Figure 31 - Temperatures for Prorotype Cylinder for First Experiment 54



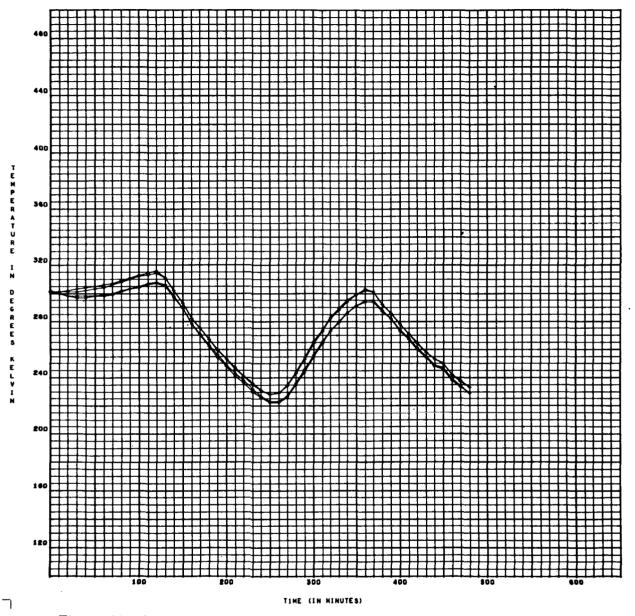


Figure 32 - Temperatures for Prototype Cylinder for Second Experiment

A SET OF EXPERIMENTS IN THERMAL SIMILITUDE

by

Billy P. Jones

and

James K. Harrison

The information in this report has been reviewed for security classification. Review of any information concerning Department of Defense or Atomic Energy Commission programs has been made by the MSFC Security Classification Officer. This report, in its entirety, has been determined to be unclassified.

This document has also been reviewed and approved for technical accuracy.

RHARD B. HELLER

Dep. Director, Research Projects Laboratory

DISTRIBUTION

Dr. Lal R-DIR Mr. Merrill Mr. Weidner Mr. Miller R-AERO Mr. Snoddy Dr. Geissler Mr Watkins Mr. Weathers R-ASTR Dr. Haeussermann MS-IPL (8) R-COMP MS-IP Dr. Hoelzer MS-IS (6) Mr. Yarborough MS-H R-COMP-GE Miss M. Morgan HME-P Mr. Emerson Whatley CC-P R-P&VE MS-T (5) Mr. Cline Scientific & Technical Information R-TEST Facility (25) Mr. Heimberg Attn: NASA Repres. (S-AK/RKJ) R-ME P. O. Box 5700 Dr. Kuers Bethesda, Maryland R-RP National Aeronautics & Space Dr. Stuhlinger Administration Mr. Heller Washington, D. C. 20546 Mr. Bucher Attn: Mr. Conrad Mook Dr. Shelton Code RV-1 Dr. Dozier Redstone Scientific Information Dr. Mechtly Center Mr. Downey Documents Section (3) Mr. Miles Dr. Schocken Mr. Arnett Greenbelt, Maryland Mr. Bannister

Mr. Fields

Mr. Gates

Mr. Jones

Mr. Fountain

Mr. Harrison

Goddard Space Flight Center Attn: Mr. Milton Schach Jet Propulsion Laboratory 4800 Oak Grove Drive Pasadena, California 91103

Attn: Dr. J. M. F. Vickers

Lewis Research Center 21000 Brookpark Road Cleveland, Ohio 44135 Attn: Dr. Herman Mark

Langley Research Center Langley Station Hampton, Virginia 23365 Attn: Dr. Samuel Katzoff

Manned Spacecraft Center Houston, Texas 77058 Attn: Mr. Jack C. Heberlig

Ames Research Center Moffett Field, California 94035 Attn: Mr. Elmer Streed

Lockheed Missiles & Space Company Palo Alto, California Attn: Mr. Robert E. Rolling

Engineering Mechanics Department University of Alabama University, Alabama Attn: Dr. J. D. Matheny

ARO, Inc.
Tullahoma, Tenn.
Attn: Mr. Dave Anderson
Mr. D. L. Adkins
Arthur D. Little Company
Acorn Park
Cambridge, Mass.
Attn: Mr. Frank Gabron

Douglas Aircraft Company, Inc. Santa Monica, California Attn: Mr. N. E. Folkman

Wright Air Development Center Wright-Patterson AFB Environmental Control Branch Vehicle Equipment Division Dayton, Ohio Attn: Mr. Carl J. Feldmanis